

HOMEWORK VII
on the material from lectures on Oct, 23 and partially Oct, 30
MATH-UA 0248-001 THEORY OF NUMBERS
due on Nov, 3, 2017

1. Determine all the primitive roots of the prime 17.
2. For a prime $p > 3$ prove that the primitive roots of p occur in pairs r, r' with $rr' \equiv 1 \pmod{p}$. (Hint: if r is a primitive root of p , consider the integer $r' = r^{p-2}$).
3. Show that $1000!$ terminates in 249 zeros.
4. Show that

$$\sum_{n=1}^N \mu(n) \lfloor N/n \rfloor = 1.$$