

**HOMEWORK XI**  
**MATH-UA 0248-001 THEORY OF NUMBERS**

due on Dec, 8, 2017

1. Determine the infinite continued fraction representation of  $\sqrt{26}$ .
2. Establish that if  $x_0, y_0$  is a solution of the equation  $x^2 - dy^2 = -1$ , then  $x = 2x_0^2 + 1, y = 2x_0y_0$  satisfies  $x^2 - dy^2 = 1$ .
3. If  $d$  is divisible by a prime  $p \equiv 3 \pmod{4}$ , show that the equation  $x^2 - dy^2 = -1$  has no solution.