

1. Find the surface area of the torus obtained from rotating the circle in yz -plane $(y - b)^2 + z^2 = a^2$ around z -axis, where $0 < a < b$ are constants

2. Evaluate

$$\iint_S x^2 z + y^2 z \, dS$$

where S is the hemisphere $x^2 + y^2 + z^2 = 4$, $z \geq 0$.

3. A surface S is parameterized by $\vec{r}(\theta, z) = (\cos \theta, \sin \theta, z)$, $0 \leq \theta \leq 2\pi$, $-1 \leq z \leq 1$. Its orientation agrees with $\frac{\partial \vec{r}}{\partial \theta} \times \frac{\partial \vec{r}}{\partial z}$
- (i). What surface is it geometrically?
- (ii). If $\vec{F}(x, y, z) = (-y, x, z)$, evaluate

$$\iint_S \vec{F} \cdot d\vec{S}$$

(iii). Can you explain the result you obtained in (ii) geometrically?

4. If S is the part of the graph of a smooth function $z = f(x, y) = 1 - x^2 - y^2$ above xy -plane with upward orientation, $\vec{F}(x, y, z) = (y, x, z)$, compute

$$\iint_S \vec{F} \cdot d\vec{S}$$

5. Evaluate the surface integral $\iint_S \vec{F} \cdot d\vec{S}$, where $\vec{F} = \langle x, -z, y \rangle$ and S is the part of the sphere $x^2 + y^2 + z^2 = 4$ in the first octant, with orientation pointing towards the origin.