

1. Find the limit

(i). $\lim_{x \rightarrow \infty} 2^{-x^2}$

(ii). $\lim_{x \rightarrow \infty} \frac{e^{3x} - e^{-3x}}{e^{3x} + e^{-3x}}$

(iii). $\lim_{x \rightarrow 3^+} \log_{\frac{1}{2}}(x^2 - 9)$

(iv). $\lim_{x \rightarrow \infty} [\ln(1 + x^2) - \ln(1 + x)]$

2. Prove that $f(x) = \frac{1 - e^{\frac{1}{x}}}{1 + e^{\frac{1}{x}}}$ is an odd function.

3. Find the inverse function of $f(x) = \frac{4x-1}{2x+3}$

4. If $f(x) = x^5 + x^3 + x$, find $(f^{-1})'(3)$

5. Compute the value of $2 \log_3 10 - \log_3 18 - \log_3 50$

6. Differentiate the following functions:

(i). $f(x) = 10^{1-x^2}$

(ii). $f(x) = x^2 e^{-\frac{1}{x}}$

(iii). $f(x) = \ln(\ln x)$

(iv). $f(x) = \log_2(\sin x^2)$