

1. Differentiate the functions:

(i). $f(x) = x^3 - \frac{1}{\sqrt[4]{x^3}}$

(ii). $f(x) = \frac{\sin x}{2} + \frac{2}{x} + 3$

(iii). $f(x) = x^3 \cos x$

(iv). $f(x) = \frac{\sqrt{x}-1}{\sqrt{x+1}}$

(v). $f(x) = x^2 \sin x \tan x$

(vi). $f(x) = \frac{\cos x}{1-\sin x}$

2. Show that the curve $y = 6x^3 + 5x - 3$ has no tangent line with slope 4.

3. Find equations of the tangent line to the curve $y = \frac{x-1}{x+1}$ that are parallel to the line $x - 2y = 2$.

4. The cost function of producing x units of goods is given by

$$C(x) = 1200 + 12x - 0.1x^2 + 0.0005x^3$$

(a). Find the marginal cost function

(b). Find $C'(200)$. What does it predict?

(c). Estimate the extra cost when the production is increased from 200 to 202.

5. A, B are constants. $y = A \sin x + B \cos x$ satisfies the equation

$$y'' + y' - 2y = 0$$

Determine the value of A and B .