

1 **Defining Sudden Stratospheric Warmings in Models: Accounting for Biases in Model Climatologies**

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12

13 **Abstract**

14 A sudden stratospheric warming (SSW) is defined by the World Meteorological Organization  
15 (WMO) as zonal-mean zonal wind reversal at 10 hPa and 60°N, associated with a reversal of the  
16 climatological temperature gradient at this elevation. This wind criteria in particular has been applied to  
17 reanalysis data and climate model output during the last few decades. In the present study, it is shown  
18 that the application of this definition to models can be affected by model mean biases; i.e., more  
19 frequent SSW appear to occur in models with a weaker climatological polar vortex. In order to overcome  
20 this deficiency, a tendency-based definition, which is not sensitive to the model mean bias, is proposed  
21 and applied to the multi-model data sets archived for the Coupled Model Intercomparison Projection  
22 phase 5 (CMIP5). In this definition, SSW-like events are defined by sufficiently strong vortex  
23 deceleration. This approach removes a linear relationship between the SSW frequency and intensity of  
24 climatological polar vortex for both the low-top and high-top CMIP5 models. Instead, the resulting SSW  
25 frequency is strongly correlated with wave activity at 100 hPa. The two definitions detect quantitatively  
26 different SSW in terms of lower stratospheric wave activity and downward propagation of stratospheric  
27 anomalies to the troposphere. However, in both definitions, the high-top models generally exhibit more  
28 frequent SSW than the low-top models. Moreover, a hint of more frequent SSW in a warm climate is  
29 commonly found.

30

31 **1. Introduction**

32 A sudden stratospheric warming (SSW) is an abrupt warming event in the polar stratosphere. It  
33 occurs mostly in mid-winter and almost exclusively in the Northern Hemisphere. During this event, the  
34 polar stratospheric temperature increases by several tens of degrees within a few days and eventually

35 becomes warmer than mid-latitude temperature. At the same time, the prevailing westerly wind slows  
36 and shifts to an easterly direction ((Quiroz 1975); (Labitzke 1977); (Andrews et al. 1987)). Based on these  
37 observations, SSWs has been often defined as a zonal-mean zonal wind reversal in the polar  
38 stratosphere. In particular, the onset of SSW is defined as the time at which the 10-hPa zonal-mean  
39 zonal wind at 60°N changes its direction from westerly to easterly during the winter (e.g., (Charlton and  
40 Polvani 2007)). This simple definition, related to that of the World Meteorological Organization (WMO),  
41 which also requires a reversal of the temperature gradient over the polar cap, effectively detects the  
42 observed characteristics of SSW ((Palmeiro et al. 2015); (Butler et al. 2015)). As Butler et al. (2015) show  
43 that the temperature gradient criterion only affects a very small number of SSWs, we will use the  
44 simpler, wind only definition from now when referring to the WMO criterion.

45         It is important to note that the WMO definition is not the only definition of extreme variability of  
46 the stratosphere. As summarized in Palmeiro et al. ((2015)) and Butler et al. ((2015)), many definitions  
47 for SSWs appear in the literature. These include an area-integrated zonal wind reversal, a tendency-  
48 based definition, a Northern Annular Mode (NAM)-based definition, an Empirical Orthogonal Function  
49 (EOF)-based definition, and a two-dimensional vortex moment analysis. Palmeiro et al. ((2015))  
50 documented that the observed frequency of SSW and the associated downward coupling are not highly  
51 sensitive to the details of the definitions, although interannual to decadal variability of SSW is somewhat  
52 sensitive (particularly the drought of SSWs in the 1990s, cf. Butler et al., (2015)). This indicates that long-  
53 term statistics of SSW are not highly sensitive to the definition of SSW. However, this is not necessarily  
54 true for climate models in which the climatology and temporal variability differ from observations.

55         Although application of the WMO definition to the climate model output is straightforward,  
56 interpretation of the results is not necessarily obvious. For example, SSWs may occur more frequently in  
57 a model if it exhibits larger variability of the polar vortex, or if the climatological polar vortex is weak in  
58 the model. In the latter case a case, relatively weak deceleration without strong wave driving can result

59 in wind reversal. As an example, Fig. 1 shows zonal-mean zonal wind at 10 hPa and 60°N during winter  
60 1994–1995 from the reanalysis data and the Coupled Model Intercomparison Project phase 5 (CMIP5)  
61 model. The reanalysis data show rapid deceleration of the zonal wind from mid-January to early  
62 February (Fig. 1a). However, the westerly does not shift to an easterly, and according to the WMO  
63 definition, this case is defined as a minor warming event rather than SSW. In the model, the polar vortex  
64 is significantly weaker than observation (Fig. 1b). Under this weak background wind, relatively weak  
65 temporal variability can easily lead to wind reversal. Thus, the model exhibits three SSW events between  
66 November and March, although the deceleration of the polar vortex is not as pronounced as the minor  
67 warming event in the reanalysis data (Fig. 1a). It is thus not obvious how a model is biased if it does not  
68 capture the correct frequency of SSWs, and worse, a model could potentially get the correct frequency  
69 for the wrong reason, a combination of a weak vortex and weak variability, or vice versa.

70 [Fig. 1 about here]

71 This result motivated us to explore the sensitivity of SSW to the model mean bias. For multi-  
72 model analysis, previous studies have typically used a WMO-like definition ((Charlton et al. 2007);  
73 (Butchart et al. 2011); (Charlton-Perez et al. 2008), (2013)). Because SSW frequency in the model,  
74 evaluated by the WMO definition, may be influenced by the model mean bias, it is questionable  
75 whether the quantitative assessment of SSW frequency in the literature is robust. Although not explored  
76 in detail, Butchart et al. ((2011)) do in fact attributed a large intermodel spread in SSW frequency in their  
77 multi-model analysis to the different intensities of the polar vortex.

78 By considering model mean bias, this work revisits the stratospheric variability and SSW frequency  
79 in the state-of-the-art climate models. Following previous studies (e.g., (Charlton-Perez et al. 2013);  
80 (Manzini et al. 2014)), the models are roughly characterized by grouping them into high-top and low-top  
81 models. The low-top models, which have a comparatively poor representation of stratospheric  
82 processes, typically underestimate the observed SSW frequency ((Charlton-Perez et al. 2013)). In this

83 study, it is shown that low-top models underestimate SSW frequency even if a different SSW definition  
84 is applied. However, the difference in SSW frequency between the high-top and low-top models  
85 becomes smaller when the model mean bias is considered.

86 This paper is organized as follows. In sections 2 and 3, the data used in this study and the  
87 definition of SSW are described. Section 4 explores the climatology, interannual variability, and SSW  
88 frequency in the historical simulations. In section 5, the results are briefly compared with scenario  
89 integrations in order to examine the potential changes in SSW frequency in a warmer climate.

90

## 91 **2. Data**

92 The daily-mean zonal-mean zonal wind and geopotential height fields were obtained from the 40-  
93 year European Centre for Medium-Range Weather Forecasts (ECMWF) Re-Analysis (ERA40; (Uppala et  
94 al. 2005)) for 45 winters of 1957–2002. The results were compared with the state-of-the-art climate  
95 models archived for CMIP5 (Table 1). All models that provide both the historical and Representative  
96 Concentration Pathway 8.5 (RCP8.5) simulations were used. Most analyses were performed for the  
97 historical runs, whereas the RCP8.5 runs were examined to evaluate possible changes in SSW frequency  
98 in a warm climate. The analysis period of RCP8.5 runs was set to 45 winters from 2044 to 2099. When  
99 multiple ensemble members were available, only the first ensemble member (r1i1p1) was used. An  
100 exception is CCSM4, for which the sixth ensemble member (r6i1p1) was used owing to incomplete data  
101 in the first ensemble member.

102 To highlight the model mean bias in the stratosphere, the CMIP5 models were grouped into two  
103 subgroups by considering the model top ((Charlton-Perez et al. 2013); (Manzini et al. 2014)). Specifically,  
104 models with tops of 1 hPa or higher were classified as high-top models; those with model tops below 1  
105 hPa were classified as low-top models. As described in Table 1, CanESM2 has a model top near 0.5 hPa.

106 It is ambiguous to place this model into either the high-top or low-top category. Following Manzini et al.  
107 ((2014)), this model was therefore classified as a mid-top model.

108 [Table 1 about here]

109 It is well documented that after an SSW, stratospheric anomalies tend to propagate downward to  
110 the troposphere and the surface. Such downward coupling is often evaluated with a so-called “dripping  
111 paint” composite of the NAM index ((Baldwin and Dunkerton 2001)). In this study, rather than using the  
112 EOF-based NAM index, however, a simple NAM index was used. The NAM index is computed by  
113 integrating the geopotential height anomalies from 60°N to the pole at each pressure level ((Cohen et al.  
114 2002); (Baldwin and Thompson 2009)). The sign is then flipped to obtain a consistent sign convention of  
115 the EOF-based NAM index. The resulting time series are then normalized by one standard deviation of  
116 the NAM index of ERA40. This ensures that the strength of the variability of one standard deviation in  
117 the model is the same as that of one standard deviation in the reanalysis datasets. Specifically, the  
118 variability in the models is comparable to that in the reanalysis.

119

### 120 **3. Definition of SSW**

121 In this study, the two definitions of SSW were adopted. A WMO-like definition, requiring a zonal-  
122 mean zonal wind reversal at 10 hPa and 60°N, was used as a reference. When an SSW was detected, no  
123 subsequent event is allowed within a 20-day interval, the period determined in consideration of the  
124 thermal damping time scale at 10 hPa. This allowed us to avoid a double counting of essentially the  
125 same event. Final warming events were removed by adopting the method proposed by Charlton and  
126 Polvani ((2007)).

127 As previously discussed, the WMO wind focused definition can be impacted by model mean bias.  
128 To reduce such dependency, a new definition based on the zonal-mean zonal wind tendency (e.g.,  
129 (Nakagawa and Yamazaki 2006); (Martineau and Son 2013)) was also applied. Specifically, an SSW-like

130 event was identified when the tendency of the zonal-mean zonal wind at 10 hPa and 60°N exceeded  
131  $-1.1 \text{ m s}^{-1} \text{ day}^{-1}$  over 30 days; that is, a change in vortex strength must exceed  $-33 \text{ m s}^{-1}$  over 30 days.  
132 The reference latitude and pressure level used in the present study are identical to those used in the  
133 WMO definition to enable direct comparison.

134 The two free parameters, i.e., the threshold value of deceleration ( $-1.1 \text{ m s}^{-1} \text{ day}^{-1}$ ) and the time  
135 window for tendency evaluation (30 days) were determined by referring to the observed SSW. The latter,  
136 a 30-day window, was inspired by the correlation analysis of Polvani and Waugh ((2004)). Polvani and  
137 Waugh ((2004)) showed that the upward wave activity entering the stratosphere, integrated over 20  
138 days or longer, leads to a marked weakening of the polar vortex. As discussed in section 4, wave activity,  
139 which drives SSW, is often maintained for about 30 day; thus, a 30-day window was selected in this  
140 study. A slight adjustment of the analysis window (e.g., 20 or 40 days) did not change the overall results,  
141 as subsequently described.

142 The minimum deceleration threshold,  $-1.1 \text{ m s}^{-1} \text{ day}^{-1}$ , is somewhat arbitrary. In this study, this  
143 threshold value was selected simply to recover the WMO wind based SSW frequency. It is known that  
144 SSW frequency in the reanalysis data, evaluated at 10 hPa using various definitions, is about 6.4 events  
145 per decade ((Butler et al. 2015); (Palmeiro et al. 2015)). The sensitivity of SSW frequency to the  
146 threshold value is also discussed subsequently.

147 It is important to note that the tendency-based definition does not consider a zonal-mean zonal  
148 wind reversal. The detected SSW therefore includes major SSW in addition to minor warming events in  
149 terms of the WMO definition. As such, the dynamical evolution of SSW in the two definitions is not  
150 necessarily the same. Table 2 presents the central dates of SSW events identified by the WMO and  
151 tendency-based definitions in ERA40. Only 17 of a total of 29 SSW events, or 60%, were common in the  
152 two definitions, which clearly indicates that the detected SSW differed significantly. A major difference  
153 appeared in early 1990s. Although no SSW events were identified for 1990 and 1997 in the WMO

154 definition, five SSW events were detected in the tendency-based definition, as clearly shown in Fig. 2.  
155 This suggests that while the vortex was abnormally strong over this decade, it was still about as variable  
156 as in other decades. Overall, the tendency-based SSW events were more evenly distributed in time. This  
157 even distribution, with no significant decadal variability, is somewhat similar to NAM-based SSW, as  
158 shown in Fig. 2 of Butler et al. ((2015)).

159 [Fig. 2 about here]

160

## 161 **4. Historical runs**

### 162 **a. Climatology and interannual variability of the polar vortex**

163 Figure 3a shows a vertical cross-section of zonal-mean zonal wind during the Northern  
164 Hemisphere winter (December–January–February, DJF) from ERA40. Westerly jets during the boreal  
165 winter consist of a tropospheric jet around 30°N and a stratospheric polar vortex around 65°N (Fig. 3a).  
166 This structure was effectively captured by the multi-model mean (MMM) of the high-top models (Fig.  
167 3d). The high-top MMM biases are less than 2 m s<sup>-1</sup> (shaded), which is not significantly different from  
168 the ERA40 data over most regions. In contrast, the low-top MMM show a stronger polar vortex than  
169 that in the reanalysis data (Fig. 3g). Their mean biases are more than 5 m s<sup>-1</sup> at 10 hPa and 40°N,  
170 indicating that the polar vortex in the low-top models is biased equatorward. Although a causal  
171 relationship is unclear, the wind and temperature biases shown in Fig. 3g could partly reflect a lack of  
172 SSWs in the low-top models, as compared with reanalyses and the high-top models ((Charlton-Perez et  
173 al. 2013)).

174 [Fig. 3 about here]

175 The low-top models also exhibit significant biases in their interannual variability. Here, interannual  
176 variability is defined by a standard deviation of the DJF-mean zonal-mean zonal wind. The high-top  
177 models effectively captured the interannual variability in the extratropical stratosphere (Fig. 3e). The



178 low-top models exhibited significantly larger errors with about 33% less interannual variability than the  
179 reanalysis data at 50 hPa and 60°N (Fig. 3h). This result, which agrees well with the findings of Charlton-  
180 Perez et al. ((2013)), is to some extent anticipated because the low-top models do not resolve realistic  
181 stratospheric processes. It is interesting to note that both high-top and low-top models underestimated  
182 tropical stratospheric variability, indicating the failure of simulating quasi-biennial oscillation (QBO; (Kim  
183 et al. 2013)). Because the QBO can influence the Northern Hemisphere wintertime stratospheric polar  
184 vortex ((Holton and Tan 1980); (Garfinkel et al. 2012)), the lack of QBO activity in the models could  
185 adversely affect extratropical stratospheric variability on interannual time scales.

186

#### 187 **b. Intraseasonal variability of the polar vortex**

188 High-top models are also more realistic than low-top models in terms of their intraseasonal  
189 variability (right panels in Fig. 3). The low-top models exhibit larger biases in intraseasonal variability  
190 than the high-top models (Figs. 3f, i). These biases are not confined within the stratosphere but extend  
191 to the troposphere in high latitudes as well. This could indicate that the poorly represented  
192 stratospheric process in the low-top models may introduce bias in the upper troposphere.

193 The relationship between the deseasonalized daily zonal-mean zonal wind variability and  
194 climatological zonal-mean zonal wind at 10 hPa and 60°N is further illustrated in Fig. 4, where the high-  
195 top and low-top models reasonably separate into two clusters. The daily variability in the high-top  
196 models is about  $12 \text{ m s}^{-1}$ , which is close to the observation of about  $13 \text{ m s}^{-1}$ . However, that in the low-  
197 top models it is only about  $8 \text{ m s}^{-1}$ , which possibly indicates less frequent SSWs. In addition, the  
198 intermodel spread of the low-top models is larger than that of the high-top models in both climatology  
199 and intraseasonal variability. This result confirms those of previous studies such that a high model top is  
200 helpful for reproducing the stratospheric mean state and temporal variability ((Charlton-Perez et al.  
201 2013); (Manzini et al. 2014)).

202 [Fig. 4 about here]

203

### 204 **c. SSW statistics**

205 Extending the results of Charlton-Perez et al. ((2013)), the SSW frequency of ERA40 was first  
206 evaluated by using the WMO wind definition (Fig. 5a). The long-term mean SSW frequency is 6.4 events  
207 per decade, as shown by the horizontal line in the figure. CMIP5 models typically underestimate this  
208 frequency ((Charlton-Perez et al. 2013)). The SSW frequency in the high-top models varies from 3 to 9  
209 events per decade (red bars). On average, the frequency was 5.8 events per decade, as shown by the  
210 rightmost red bar in the figure, which is reasonably close to the reference frequency. In contrast, the  
211 low-top models exhibit only up to 4 events per decade (blue bars in the figure), with 1.8 events per  
212 decade on average (rightmost blue bar). This result is significantly smaller than the high-top MMM  
213 frequency. More importantly, the intermodel spread in the two groups of models does not overlap,  
214 indicating that the low-top models are well separated from the high-top models in terms of SSW  
215 frequency, as also shown in Fig. 4. This result supports the findings of Charlton-Perez et al. ((2013)), who  
216 analyzed a slightly smaller numbers of CMIP5 models. Somewhat surprisingly, the mid-top model,  
217 CanESM2, showed significantly more frequent SSW events than those in other models, with 10.7 events  
218 per decade. Such high frequency is associated with a weak background wind in this model, as illustrated  
219 in Figs. 1b and 4.

220 [Fig. 5 about here]

221 The SSW frequency was also evaluated using the tendency-based definition (Fig. 5b). By  
222 construction, the SSW frequency under this definition remains 6.4 events per decade in ERA40. Although  
223 each model shows SSW frequencies that differed from the WMO definition, the high-top MMM was 6.2  
224 events per decade, which is quantitatively similar to the observed frequency. Within the uncertainty  
225 range, this frequency is also similar to that derived from the WMO definition: the SSW frequency in the

226 WMO definition is 5.8 events per decade (Fig. 5a), whereas the tendency-based definition illustrates 6.2  
227 events per decades (Fig. 5b). However, the intermodel spread is only half of that of the WMO definition.  
228 This suggests that the tendency-based definition is less sensitive to intermodal differences (i.e. biases) as  
229 the WMO definition.

230 The low-top models again exhibited fewer frequent SSW events than the high-top models, with an  
231 MMM frequency of 3.7 events per decade. This result indicates that regardless of the definition, the  
232 low-top models tend to underestimate the observed SSW frequency. Here, it is important to note that  
233 the resulting SSW frequency was larger than that derived from the WMO definition in Fig. 5a, (i.e., 1.8  
234 events per decade), which indicates that the different SSW frequencies between the high-top and low-  
235 top models become smaller when a definition free of model mean bias is used. In fact, the intermodel  
236 spread of SSW frequency in the low-top models overlaps that in the high-top models, as shown in Fig.  
237 5b. This result indicates that extreme event frequency may be less sensitive to the model top than that  
238 previously reported (e.g., (Charlton-Perez et al. 2013)). This is particularly true if the two models with  
239 extremely rare SSW events (i.e., CSIRO-Mk3-6-0 and INMCM4) are excluded from the low-top MMM.

240 The only mid-top model, CanESM2, shows a significant reduction in SSW frequency from the  
241 WMO definition to the tendency-based definition, as indicated by the green bars in Figs. 5a and b. When  
242 the tendency-based definition is used, the SSW frequency is close to the observed frequency. As noted  
243 in section 3, the model classification is based a model top above or below 1 hPa: CanEMS2, in which the  
244 model top is 0.5 hPa, was a clear outlier belonging to neither high-top nor low-top models when the  
245 WMO definition was used (Fig. 5a). When the tendency-based definition was used, the SSW frequency  
246 of this model became similar to that of the high-top models.

247 Both the WMO wind only and tendency-based definitions utilize zonal-mean zonal wind at a fixed  
248 latitude (60°N) to evaluate the polar vortex weakening. This latitude corresponds to the vortex boundary  
249 in the reanalysis data ((Butler et al. 2015)). However, the same may not be true when using the models.

250 In fact, as shown in Fig. 3, the latitudinal structure of polar vortex in the model differs from that in the  
251 reanalysis data, and 60°N is not the vortex boundary in all models. This is particularly true for the low-  
252 top models (Fig. 3c). To test this possibility, all analyses were repeated by replacing the fixed reference  
253 latitude with the model-dependent reference latitudes. The latitude of the maximum zonal-mean zonal  
254 wind at 10 hPa in long-term climatology was chosen for each model, and the SSW frequency again  
255 evaluated. This modification results in an increased SSW frequency of about half an event per decade in  
256 both the high-top and low-top models (not shown). However, the overall conclusion of more frequent  
257 SSW in high-top models than those in low-top models does not change.

258 We also tested the sensitivity of the tendency-based SSW to the threshold value of deceleration  
259 and the time window for tendency evaluation. The top panel in Fig. 6 presents the SSW frequency  
260 calculated from ERA40 as a reference. As would be expected, the SSW frequency generally increased as  
261 the threshold value decreases (i.e., SSW was more frequent for a weaker threshold value). The SSW  
262 frequency also decreases with an increase in the time window. Notably, the SSW frequency in the high-  
263 top models is comparable to that in ERA40 if the observed SSW frequency of 6–8 events per decade was  
264 selected as a reference (near-zero line in Fig. 6c), but would be biased high (low) if stricter (weaker)  
265 criteria are applied. The low-top models, however, exhibited a significantly smaller number of SSW  
266 events (Fig. 6d) under all conditions. This underestimation is not highly sensitive to the parameters used  
267 in the tendency-based SSW definition. Figure 6b further shows the differences in SSW frequency  
268 between the high-top and low-top models. In general, the high-top models showed more frequent SSW,  
269 which indicates that the SSW frequency difference between the two groups of models is quite robust.

270 [Fig. 6 about here]

271 The above results are all based on intercomparison of high-top and low-top models. Individual  
272 models, however, are fundamentally different in many aspects such as dynamic core, physics,  
273 resolution, and ocean models; therefore, direct comparison of these models may not be

274 straightforward. In this regard, comparison of two different experiments from the same modeling  
275 institutes can be useful. As indicated in Table 1, The Centro Euro-Mediterraneo sui Cambiamenti  
276 Climatici (CMCC) provides two experiments: that with a climate model (CMCC-CM) and that with a  
277 climate model including a stratospheric component (CMCC-CMS). The former is a low-top version,  
278 whereas the latter is a high-top version. Figure 5b shows that CMCC-CMS exhibits realistic SSW  
279 frequency and significantly more frequent SSW than CMCC-CM, which is consistent with MMM  
280 comparison. A pair of experiments from Institut Pierre Simon Laplace Climate model 5A (IPSL-CM5A)  
281 including IPSL-CM5A-low resolution (LR) and IPSL-CM5A-medium resolution (MR), which differ in  
282 horizontal resolution, further shows that the model with higher horizontal resolution (IPSL-CM5A-MR)  
283 has more frequent SSW than IPSL-CM5A-LR. However, MPI-ESM-LR and MPI-ESM-MR, which have  
284 different vertical resolutions but the same model top, show a similar SSW frequency. A comparison of  
285 the Model for Interdisciplinary Research on Climate-Earth System Model (MIROC-ESM) and that coupled  
286 with atmospheric chemistry (MIROC-ESM-CHEM), the latter of which considers interactive chemistry in  
287 the stratosphere, also exhibited no significant difference. These results may suggest that SSW frequency  
288 is more sensitive to the model top and horizontal resolution than to vertical resolution and interactive  
289 chemistry. Additional modeling studies with systematic varying of model configurations are needed to  
290 confirm this finding.

291 To highlight the dependency of SSW frequency to the model mean bias, Fig. 7a illustrates the  
292 relationship between DJF-mean zonal-mean zonal wind at 10 hPa and 60°N and SSW frequency derived  
293 from the WMO wind definition. The high-top, mid-top, and low-top models are indicated in red, green,  
294 and blue, respectively, whereas ERA40 is shown by a black dot. A strong negative correlation was  
295 evident with a correlation coefficient of  $-0.63$ , which is statistically significant at the 95% confidence  
296 level. This clearly indicates that SSW occurred less frequently as the background wind becomes stronger  
297 (or, alternatively, fewer SSW leads to a stronger vortex). Such negative correlation was somewhat weak

298 in the low-top models owing to a few outliers that had almost no SSW events. Without these outliers  
299 (i.e., CSIRO-MK3-6-0 and MIROC5), the negative correlation is statistically significant.

300 [Fig. 7 about here]

301 Figure 7a again shows that the high-top models are well separated from the low-top models.  
302 Except for two models, most low-top models exhibited a stronger polar vortex than that by ERA40. This  
303 does not allow a wind reversal unless stratospheric wave driving is sufficiently strong (or may inhibit the  
304 resonant, vortex splitting mechanism that depends less on the wave driving; Esler and Scott (2005)). This  
305 result confirms that the difference between the high-top and low-top models shown in Fig. 5a is caused  
306 partly by the model mean biases. Another factor that may explain the less frequent SSW in the low-top  
307 models is relative weak wave driving. As shown in Fig. 7c, the low-top models exhibit somewhat weaker  
308 wave activity than the high-top models. Here, wave activity was quantified by integrating the zonal-  
309 mean eddy heat flux at 100 hPa over 40–70°N.

310 The right-hand panels of Fig. 7 are identical to those on the left except for the tendency-based  
311 definition. The linear relationship, evident in Fig. 7a, essentially disappears (Fig. 7b). Although the low-  
312 top models show a statistically significant correlation, the correlation coefficient is positive, which is  
313 largely attributed to the two outliers at the bottom left-hand corner. This result suggests that the  
314 tendency-based SSW definition is almost independent from any model mean climatological bias. More  
315 importantly, the tendency-based definition is strongly correlated with the wave activity at 100 hPa (Fig.  
316 7d) such that more frequent SSW occurs when the wave activity in the lower stratosphere is stronger.  
317 This result indicates that the tendency-based definition is more dynamically constrained than the WMO  
318 wind based definition. It should be noted that most models tend to underestimate wave activity in the  
319 lower stratosphere. This result is consistent with the fact that most models underestimate the SSW  
320 frequency regardless of the model top (Fig. 5b).

321 The relationship among the SSW frequency, daily zonal-mean zonal wind variability, and DJF mean  
322 zonal-mean zonal wind at 10 hPa and 60°N is summarized in Fig. 8, which combines the essential results  
323 of Fig. 4, 7a, and 7b. The CMIP5 models generally have realistic time-mean polar vortices but too little  
324 variability (e.g., climatology of 25–35 m s<sup>-1</sup> in Fig. 8). Under both the WMO and tendency definitions,  
325 they exhibit less frequent SSW with larger intraseasonal variability. The tendency definition clearly  
326 exhibits a more linear relationship between the SSW frequency and intraseasonal variability of the polar  
327 vortex than that by the WMO definition. Hence changes in SSW frequency can also result in variation of  
328 intraseasonal variability in a model.

329 [Fig. 8 about here]

330

#### 331 **d. SSW dynamics**

332 The SSW events identified by the two definitions can have different dynamical evolution. For  
333 example, linear wave dynamics suggest that vertical propagation of planetary-scale waves, which drive  
334 SSW, can be restricted if the zonal wind in the stratosphere becomes easterly. However, this may not be  
335 the case in the tendency-based SSW because wind reversal to easterly is not guaranteed. To address this  
336 issue, we investigated the wave activity over the course of an SSW. Figure 9 presents a composite of the  
337 temporal evolution of a zonal-mean eddy heat flux at 100 hPa integrated over 45–75°N for the two SSW  
338 definitions. The heat flux increases before the onset of an SSW, then rapidly decreases afterward.  
339 Although the evolution of wave activity is qualitatively similar in the two definitions, the tendency-based  
340 definition showed a somewhat slower decay, as shown by the black lines in Fig. 9. This result indicates  
341 that some planetary-scale waves propagated into the stratosphere even after SSW, which is consistent  
342 with the linear dynamics.

343 [Fig. 9 about here]

344 Wind-reversal SSW is associated with slightly stronger and more concentrated wave forcing than  
345 that the tendency-based SSW. However, the time-integrated wave activity over 30 days before the onset  
346 of SSW is comparable in the two definitions, indicating similar net wave driving. Figure 9 also shows that  
347 the wave activity in the high-top models is somewhat stronger than that in the low-top models from lag  
348 -20 to 0 days. Consistent with this result, the intensity of SSW events in terms of zonal wind  
349 deceleration is somewhat stronger in the high-top models than that in the low-top models (not shown).  
350 This result suggests that improved vertical resolution is helpful in simulating more realistic SSWs.

351 As discussed previously, SSWs have received much attention in recent decades because of its  
352 influence on tropospheric circulation and surface climate ((Baldwin and Dunkerton 2001)). By comparing  
353 a subset of CMIP5 models, Charlton-Perez et al. ((2013)) reported that high-top models tend to have  
354 more persistent anomalies than low-top models in the troposphere. In Fig. 10, a similar comparison is  
355 made in terms of NAM-index anomalies for the two SSW definitions. For ERA40, the tendency-based  
356 SSW exhibited a stronger phase change than the wind-reversal SSW in the NAM anomalies in both the  
357 lower stratosphere and the troposphere (Figs. 10a, b), but an overall weaker (less negative) tropospheric  
358 NAM response following the event. Such a difference is also evident in the MMM. These results suggest  
359 that the SSWs identified by the two definitions are indeed quantitatively different. However, the overall  
360 evolution of SSW and the associated wave driving and downward propagation are qualitatively similar.

361 [Fig. 10 about here]

362 It is important to note that SSW-induced NAM-index anomalies in the lower stratosphere tend to  
363 persist longer in the high-top models than those in the low-top models (Fig. 10). Similarly, the  
364 tropospheric anomalies are stronger and persisted slightly longer in the high-top models than in the low-  
365 top models in the two definitions. This result suggests that the timescale of SSW and downward  
366 coupling are somewhat sensitive to the model top.

367



## 368 5. SSWS in future climate projections

369 We now compare the SSW frequency in the recent past with that in the 21st century. Figure 11  
370 illustrates the projected changes in SSW frequency under the RCP8.5 scenario by the end of 21st  
371 century. The WMO definition suggests slightly more frequent SSW in the warm climate (Fig. 11a), which  
372 agrees well with the results of Charlton-Perez et al. ((2008)). The high-top models generally exhibited a  
373 more positive trend in SSW frequency than the low-top models; 8 out of 12 high-top models showed an  
374 increasing trend (Fig. 11c). However, the low-top models did not show a clear trend if CSIRO-MK3-6-0,  
375 which failed to simulate SSW, was excluded. Half of the low-top models showed increasing and  
376 decreasing trends, respectively.

377 [Fig. 11 about here]

378 McLandress and Shepherd ((2009)) suggested that the increase in SSW frequency in a warmer  
379 climate, as reported by Charlton-Perez et al. ((2008)), may be partly attributed to changes in background  
380 wind rather than those in wave activity. By applying a relative definition, they showed that SSW  
381 frequency did not change significantly in their model. This idea is evaluated in Fig. 11b with the  
382 tendency-based SSW definition. Consistent with the historical simulations, the high-top models capture  
383 the observed SSW frequency reasonably well. However, in both groups of models, a weak positive trend  
384 in the SSW frequency is observed (Fig. 11b). Although the absolute change is not statistically significant,  
385 21 of 27 CMIP5 models exhibited an increasing trend (Fig. 11d). Such behavior was evident upon  
386 separate examination of the high-top and low-top models, with 9 of 12 high-top and 11 of 14 low-top  
387 models showing increasing trends. This result may imply that some dynamical properties of SSW, such  
388 as planetary wave activity, may change in the future. To identify the dynamical mechanisms, further  
389 analyses are needed.

390

## 391 **6. Summary and discussion**

392       The present study suggests that the wind metric emphasized by the WMO definition of an SSW --  
393 a wind reversal at 10 hPa and 60°N -- can be impacted by model mean biases ((McLandress and  
394 Shepherd 2009)). The definition can straightforwardly be applied to models, but the interpretation may  
395 be more complicated. If the climatological polar vortex of the model is stronger than observation, it  
396 tends to allow less frequent SSWs. Such a relationship is robustly found in the CMIP5 models, indicating  
397 that the previous multi-model studies on wind-reversal SSW are likely influenced by the model mean  
398 biases and long-term mean flow changes.

399       An alternative definition of extreme vortex variability, aimed at making it independent of model  
400 mean biases, was proposed in this study. This definition detects SSWs by examining the zonal-mean  
401 zonal wind tendency at 10 hPa and 60°N. In this definition, the linear relationship between SSW  
402 frequency and the intensity of climatological polar vortex, which is evident in the WMO definition,  
403 essentially disappears. More importantly, the SSW frequency becomes highly correlated with wave  
404 activity at 100 hPa. This result indicates that the tendency-based definition is more dynamically  
405 constrained than the WMO definition.

406       The tendency-based definition resulted in more frequent SSWs than the WMO definition in the  
407 climate models, particularly in the low-top models, even though it was constructed to have no effect on  
408 the frequency in ERA-40 reanalysis. This indicates that the significant difference in SSW frequency  
409 between the low-top and high-top models reported in previous studies ((Charlton-Perez et al. 2013)) can  
410 be attributed, at least partly, to model mean bias rather than wave driving. However, in both definitions,  
411 the high-top models exhibited more frequent SSW than the low-top models, consistent with stronger  
412 lower-stratospheric wave activities in the high-top models. This result indicates that a high model top  
413 and more accurate stratospheric representation are necessary for simulating realistic SSW. It was also  
414 found that in both definitions, the SSW frequency tended to increase in a warm climate. These results

415 are qualitatively consistent with those in previous studies (Charlton-Perez et al., (2008), (2013)),  
416 although their a quantitative differences. It is important to note that the SSW detected by the different  
417 definitions may have different dynamical and physical properties ((Martineau and Son 2015)). In fact,  
418 wind-reversal SSW events exhibit evolution that differs quantitatively from the tendency-based SSW.  
419 The former is associated with more focused and stronger wave activity than the latter. This difference  
420 leads to slightly longer persistence of stratospheric anomalies and a stronger downward coupling in the  
421 tendency-based SSW. Such differences need to be considered in comparisons.

422 It should be emphasized that development of a new SSW definition is not our primary intent in  
423 this study. Our objectives were to re-examine the SSW frequency in CMIP5 models by considering the  
424 model mean bias and to test the robustness of previous studies by applying the different SSW  
425 definitions. Certainly, other approaches can be used to define stratospheric extreme events that are free  
426 from model mean biases. Among various SSW definitions ((Butler et al. 2015)), however, the tendency-  
427 based definition is likely one of the simplest approaches that can be easily compared with the WMO  
428 definition. Because the zonal-mean zonal wind tendency is directly related to divergence in eddy heat  
429 flux and momentum flux in the transformed Eulerian mean equation, the tendency-based SSW is closely  
430 associated with accumulated wave activity in the stratosphere.

431 The tendency-based definition has other advantages over the WMO definition with respect to  
432 evaluation of models. The tendency-based definition is may be useful for detecting SSW in a changing  
433 climate. Previous studies have reported a possible weakening of the polar vortex in response to  
434 increasing greenhouse gas concentration (McLandress and Shepherd (2009); Manzini et al. (2014)).  
435 Because the background wind becomes weaker, the chances of a wind reversal may increase, resulting  
436 in more frequent SSW when the WMO definition is used. Such an increase in SSW frequency, however,  
437 could be misleading if the wave forcing does not change systematically (McLandress and Shepherd

438 2009). Therefore, further discussion on simple, but objective detection of stratospheric extreme events,  
439 including vortex weakening events such as SSWs, is important (Butler et al. 2015).

440

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500 **Tables**

501 Table 1 CMIP5 models used in this study and their classification.

502

503 Table 2 Sudden stratospheric warming (SSW) identified from the wind reversal and wind tendency  
504 definitions.

505

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506

## 507 **Figures**

508 Fig. 1 Zonal-mean zonal winds ( $\text{m s}^{-1}$ ) at 10 hPa and  $60^\circ\text{N}$  for (a) ERA40 and (b) CanESM2 models. The  
509 thin line across the x-axis denotes the  $0 \text{ m s}^{-1}$  threshold.

510

511 Fig. 2 Time series of major midwinter sudden stratospheric warming (SSW) events as defined using the  
512 wind reversal definition (left) and the wind tendency definition (right).

513

514 Fig. 3 (top left) Latitude and height cross-section of the climatological zonal-mean zonal winds ( $[u]$ ;  $\text{m}$   
515  $\text{s}^{-1}$ ) averaged from December to February (DJF) in ERA40. The contour interval is  $10 \text{ m s}^{-1}$ , and the zero  
516 line is indicated with a thick black line. (center and right) Same as the top left panel but for interannual  
517 variability of the DJF-mean  $[u]$  (center) and daily variability of  $[u]$  in DJF (right). For the daily variability,  
518 the mean value for each winter was subtracted from daily anomalies to remove the impact of the  
519 interannual variability. (middle and bottom rows) Same as the top row but for high-top (middle) and  
520 low-top (bottom) models. Statistically insignificant (t-test;  $p > 0.05$ ) values are hatched, and difference  
521 from ERA40 (model-ERA40) is shown by shading.

522

523 Fig. 4 Scatter plot of the zonal-mean zonal wind climatology at 10 hPa and at  $60^\circ\text{N}$  and its daily standard  
524 deviation from CMIP5 models. Red, green, blue, and black colors indicate high-top, mid-top, and low-top  
525 models and ERA40 reanalysis, respectively. Solid lines range  $\pm 1$  standard deviation among models while  
526 centered on their multi-model mean.

527

528 Fig. 5 Sudden stratospheric warming (SSW) frequency derived from (a) the wind reversal definition and  
529 (b) the wind tendency definition. Low-top, mid-top, and high-top models are colored blue, green, and



530 red, respectively. The SSW frequency in ERA40 is indicated by the black horizontal line. Multi-model  
531 mean frequency and intermodel spread (1 standard deviation) are shown at the right of each panel.  
532  
533 Fig. 6 (a) Sudden stratospheric warming (SSW) frequency as a function of the threshold value of the  
534 zonal-mean zonal wind tendency at 10 hPa and 60°N and the evaluated time window for ERA40. (b)  
535 Difference between the high-top and low-top models. Difference between ERA40 and (c) high-top and  
536 (d) low-top models. Values statistically insignificant at the 95% confidence level are hatched. The two  
537 low-top models were ignored because their SSW events are extremely rare. The SSW frequency of six to  
538 eight events per decade from ERA40 is shown by with thick black lines in each panel. The numbers at the  
539 upper right corner in each panel indicates SSW frequency or its difference from ERA40 when the  $-1.1 \text{ m}$   
540  $\text{s}^{-1} \text{ day}^{-1}$  threshold and 30-day time window are used.

541  
542 Fig. 7 (Top) Scatter plot of climatological zonal-mean zonal wind at 10 hPa and 60°N and sudden  
543 stratospheric warming (SSW) frequency for the wind reversal definition (left) and the wind tendency  
544 definition (right). (Bottom) Same as top panels but for eddy heat flux at 100 hPa integrated over 45–  
545 75°N. Low-top, mid-top, and high-top models are colored blue, green, and red, respectively. Black-  
546 dotted lines indicate the reference values in ERA40. The numbers shown in each panel denote the  
547 correlation coefficients for all (black), high-top (red), and low-top (blue) models. Statistically significant  
548 correlation coefficient at the 95% confidence level is indicated by the asterisk.

549  
550 Fig. 8 Same as Fig. 4 but for sudden stratospheric warming (SSW) frequency introduced using the wind  
551 reversal definition (left) and the wind tendency definition (right). The circle size indicates the SSW  
552 frequency.

553

554 Fig. 9 Multi-model mean time series of zonal-mean eddy heat flux at 100 hPa integrated over 45–75°N  
555 during sudden stratospheric warming (SSW) detected by the wind reversal definition (left) and the wind  
556 tendency definition (right). Lag zero indicates the onset of SSW. Low-top and high-top models are  
557 denoted by blue and red colors, respectively. The reference time series, derived from ERA40, is shown in  
558 black.

559  
560 Fig. 10 Time-height development of the northern annular mode (NAM) index during sudden  
561 stratospheric warming (SSW) events, as detected by the wind reversal definition (left) and the wind  
562 tendency definition (right) for ERA40 (top), high-top (middle), and low-top (bottom) models. The NAM  
563 index is based on polar-cap averaged geopotential height (>60°N). Shading interval of 1.0 is indicated by  
564 a white line. Hatching shows insignificant values (95%) when the multi-model spread is considered.

565  
566 Fig. 11 (Top) Same as Fig. 5 but for RCP8.5 runs. (Bottom) Difference in sudden stratospheric warming  
567 (SSW) frequency between RCP8.5 and historical runs.

568

568

569 Table 1 CMIP5 models used in this study and their classification.

Model Name	Center	Vertical Level	Model Top	Classification
ACCESS1-0	ACCESS	38	39 km	Low
ACCESS1-3	ACCESS	38	39 km	Low
BCC-CSM1-1	BCC	26	2.917 hPa	Low
BCC-CSM1-1-M	BCC	26	2.917 hPa	Low
BNU-ESM	GCESS/BNU	26	2.194 hPa	Low
CanESM2	CCC	35	0.5 hPa	Mid
CCSM4	NCAR	27	2.194 hPa	Low
CMCC-CESM	CMCC	39	0.01 hPa	High
CMCC-CM	CMCC	31	10 hPa	Low
CMCC-CMS	CMCC	95	0.01 hPa	High
CNRM-CM5	CNRM	31	10 hPa	Low
CSIRO-Mk3-6-0	CSIRO/QCCCE	18	4.5 hPa	Low
FGOALS-g2	LASG/IAP	26	2.194 hPa	Low
GFDL-CM3	GFDL	48	0.01 hPa	High
GFDL-ESM2G	GFDL	24	3 hPa	Low
GFDL-ESM2M	GFDL	24	3 hPa	Low
HadGEM2-CC	MOHC	60	84 km	High
INMCM4	INM	21	10 hPa	Low
IPSL-CM5A-LR	IPSL	39	0.04 hPa	High
IPSL-CM5A-MR	IPSL	39	0.04 hPa	High
IPSL-CM5B-LR	IPSL	39	0.04 hPa	High
MIROC5	MIROC	40	3 hPa	Low
MIROC-ESM	MIROC	80	0.0036 hPa	High
MIROC-ESM-CHEM	MIROC	80	0.0036 hPa	High
MPI-ESM-LR	MPI	47	0.01 hPa	High
MPI-ESM-MR	MPI	95	0.01 hPa	High
MRI-CGCM3	MRI	48	0.01 hPa	High
NorESM1-M	NCC	26	3.54 hPa	Low

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571

572 Table 2 Sudden stratospheric warming (SSW) identified from the wind reversal and wind tendency  
 573 definitions.

Number	Central dates	
	WMO	tendency
1	31 Jan 1958	30 Jan 1958
2	17 Jan 1960	18 Jan 1960
3	28 Jan 1963	27 Jan 1963
4	16 Dec 1965	
5	23 Feb 1966	27 Feb 1966
6	7 Jan 1968	2 Jan 1968
7	28 Nov 1968	
8	13 Mar 1969	
9	2 Jan 1970	6 Jan 1970
10	18 Jan 1971	15 Jan 1971
11	20 Mar 1971	
12		28 Feb 1972
13	31 Jan 1973	1 Feb 1973
14		28 Feb 1974
15	9 Jan 1977	
16		2 Feb 1978
17		27 Jan 1979
18	22 Feb 1979	27 Feb 1979
19	1 Mar 1980	
20		31 Jan 1981
21	4 Mar 1981	
22	4 Dec 1981	
23		31 Jan 1983
24	24 Feb 1984	19 Feb 1984
25	1 Jan 1984	
26		3 Jan 1985
27	23 Jan 1987	24 Jan 1987
28	8 Dec 1987	10 Dec 1987
29	14 Mar 1988	
30	21 Feb 1989	11 Feb 1989
31		15 Feb 1990
32		4 Feb 1991
33		16 Jan 1992
34		18 Feb 1993
35		27 Jan 1995
36	15 Dec 1998	19 Dec 1998
37	26 Feb 1999	28 Feb 1999
38	20 Mar 2000	
39	11 Feb 2001	9 Feb 2001
40	31 Dec 2001	2 Jan 2002

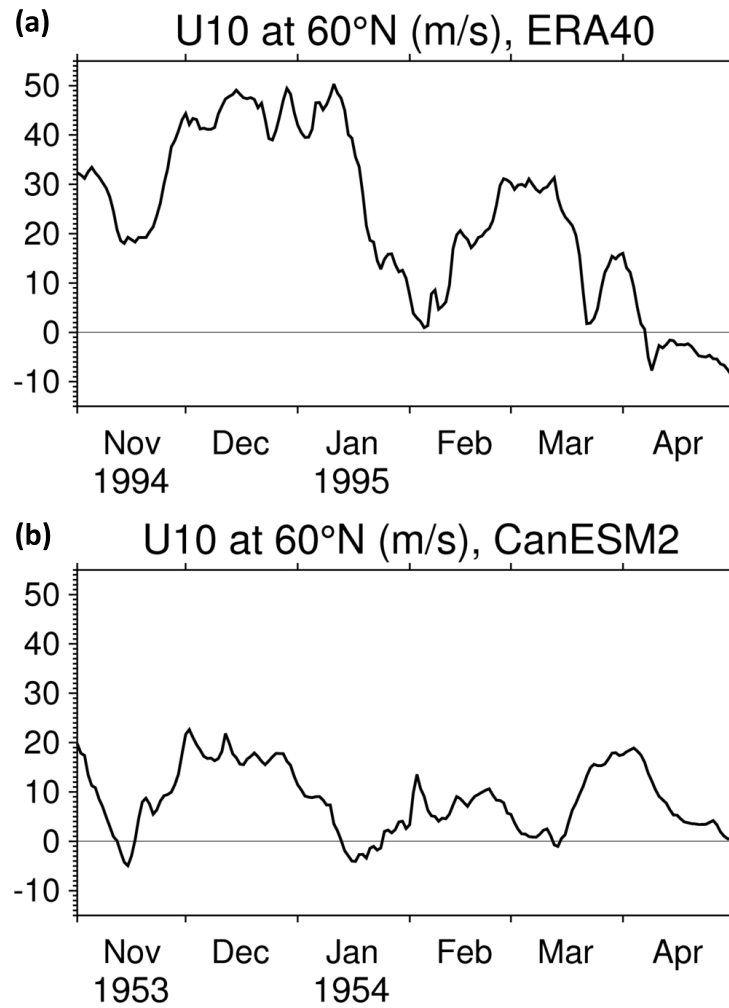


Fig. 1 Zonal-mean zonal winds ( $\text{m s}^{-1}$ ) at 10 hPa and 60°N for (a) ERA40 and (b) CanESM2 models. The thin line across the x-axis denotes the  $0 \text{ m s}^{-1}$  threshold.

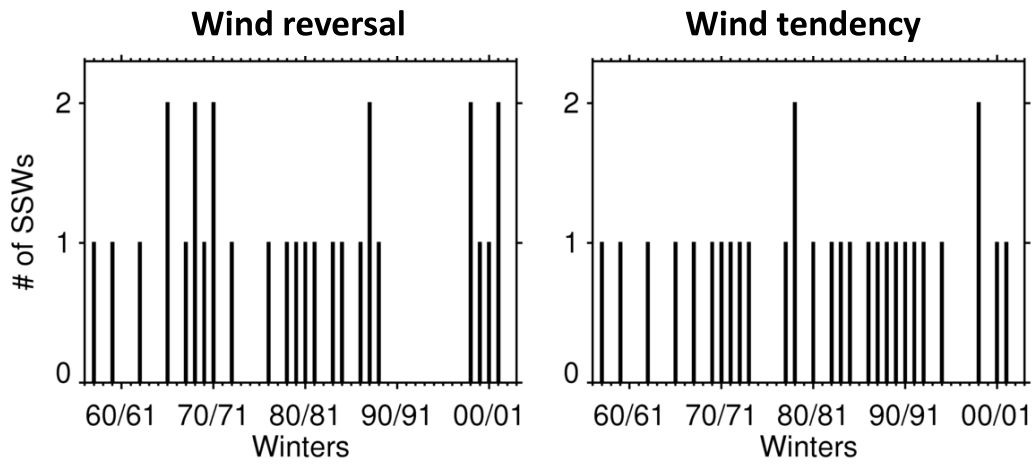
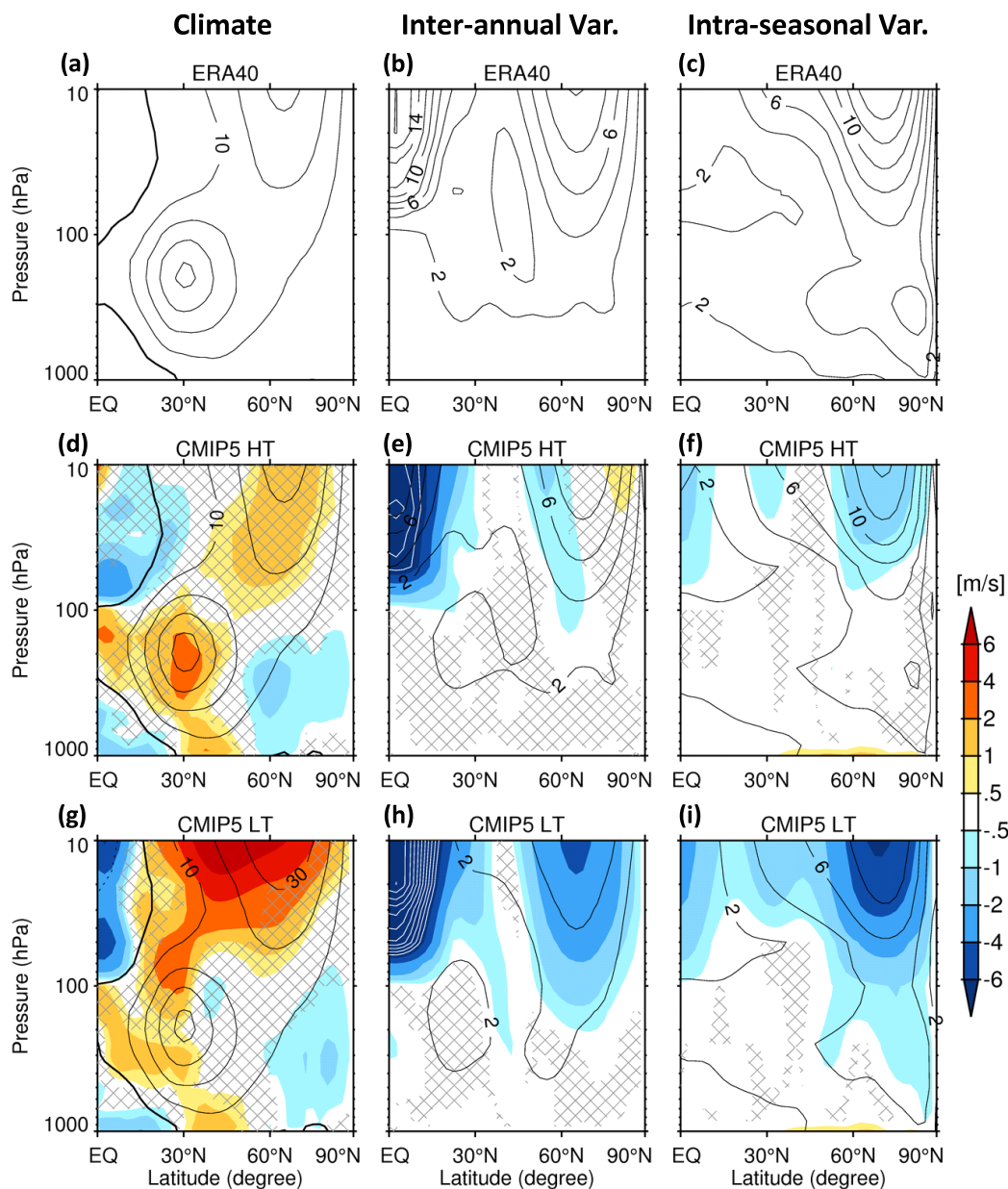


Fig. 2 Time series of major midwinter sudden stratospheric warming (SSW) events as defined using the wind reversal definition (left) and the wind tendency definition (right).



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Fig. 3 (top left) Latitude and height cross-section of the climatological zonal-mean zonal winds ( $[u]$ ;  $\text{m s}^{-1}$ ) averaged from December to February (DJF) in ERA40. The contour interval is  $10 \text{ m s}^{-1}$ , and the zero line is indicated with a thick black line. (center and right) Same as the top left panel but for interannual variability of the DJF-mean  $[u]$  (center) and daily variability of  $[u]$  in DJF (right). For the daily variability, the mean value for each winter was subtracted from daily anomalies to remove the impact of the interannual variability. (middle and bottom rows) Same as the top row but for high-top (middle) and low-top (bottom) models. Statistically insignificant ( $t$ -test;  $p > 0.05$ ) values are hatched, and difference from ERA40 (model-ERA40) is shown by shading.

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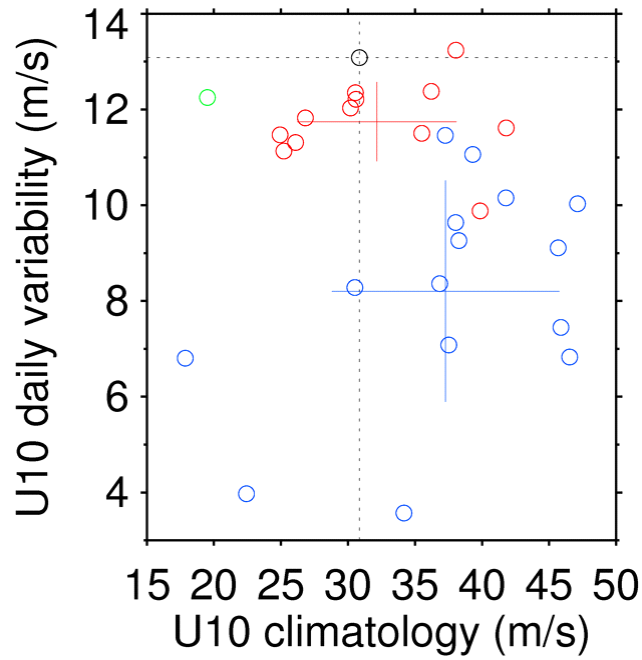


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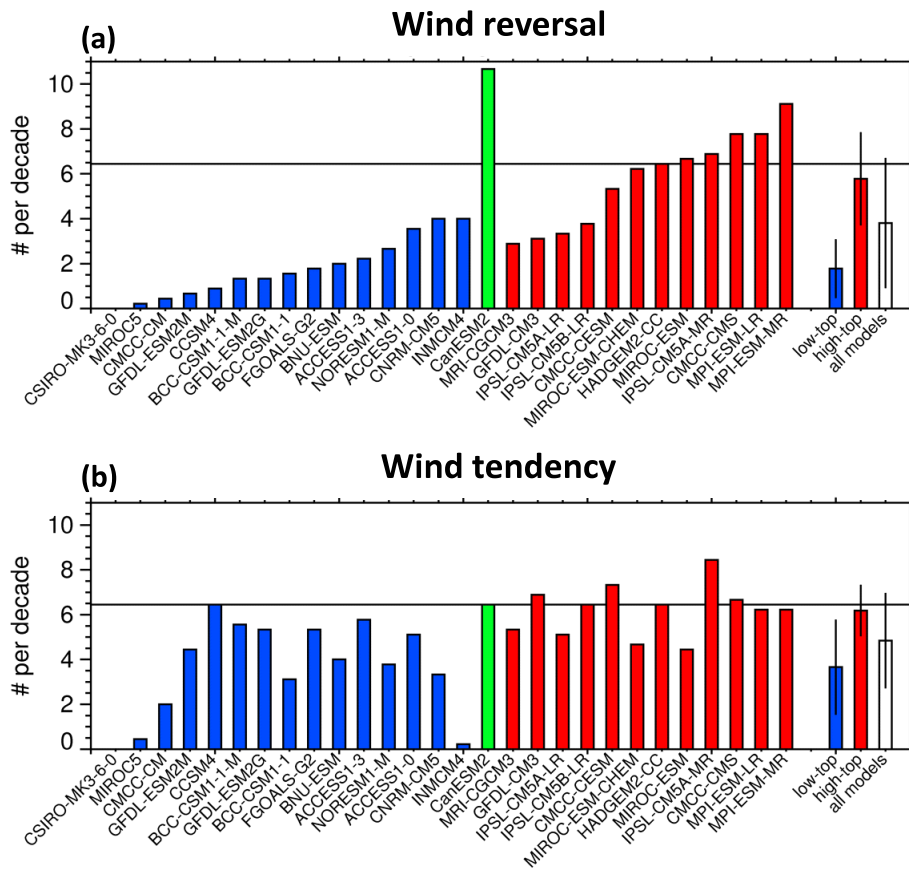


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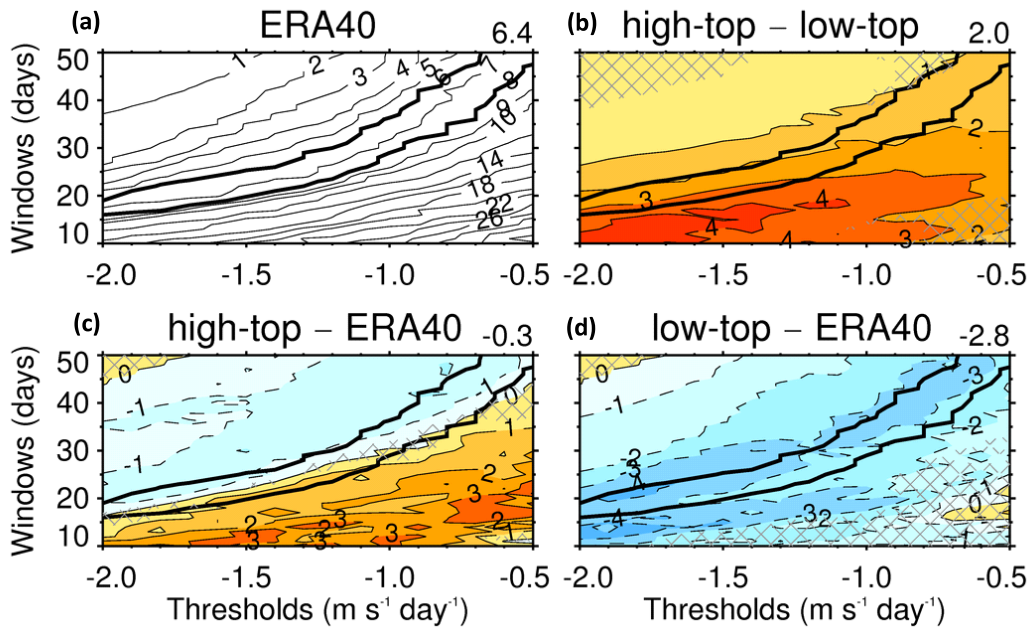


Fig. 6 (a) Sudden stratospheric warming (SSW) frequency as a function of the threshold value of the zonal-mean zonal wind tendency at 10 hPa and 60°N and the evaluated time window for ERA40. (b) Difference between the high-top and low-top models. Difference between ERA40 and (c) high-top and (d) low-top models. Values statistically insignificant at the 95% confidence level are hatched. The two low-top models were ignored because their SSW events are extremely rare. The SSW frequency of six to eight events per decade from ERA40 is shown by with thick black lines in each panel. The numbers at the upper right corner in each panel indicates SSW frequency or its difference from ERA40 when the  $-1.1 \text{ m s}^{-1} \text{ day}^{-1}$  threshold and 30-day time window are used.

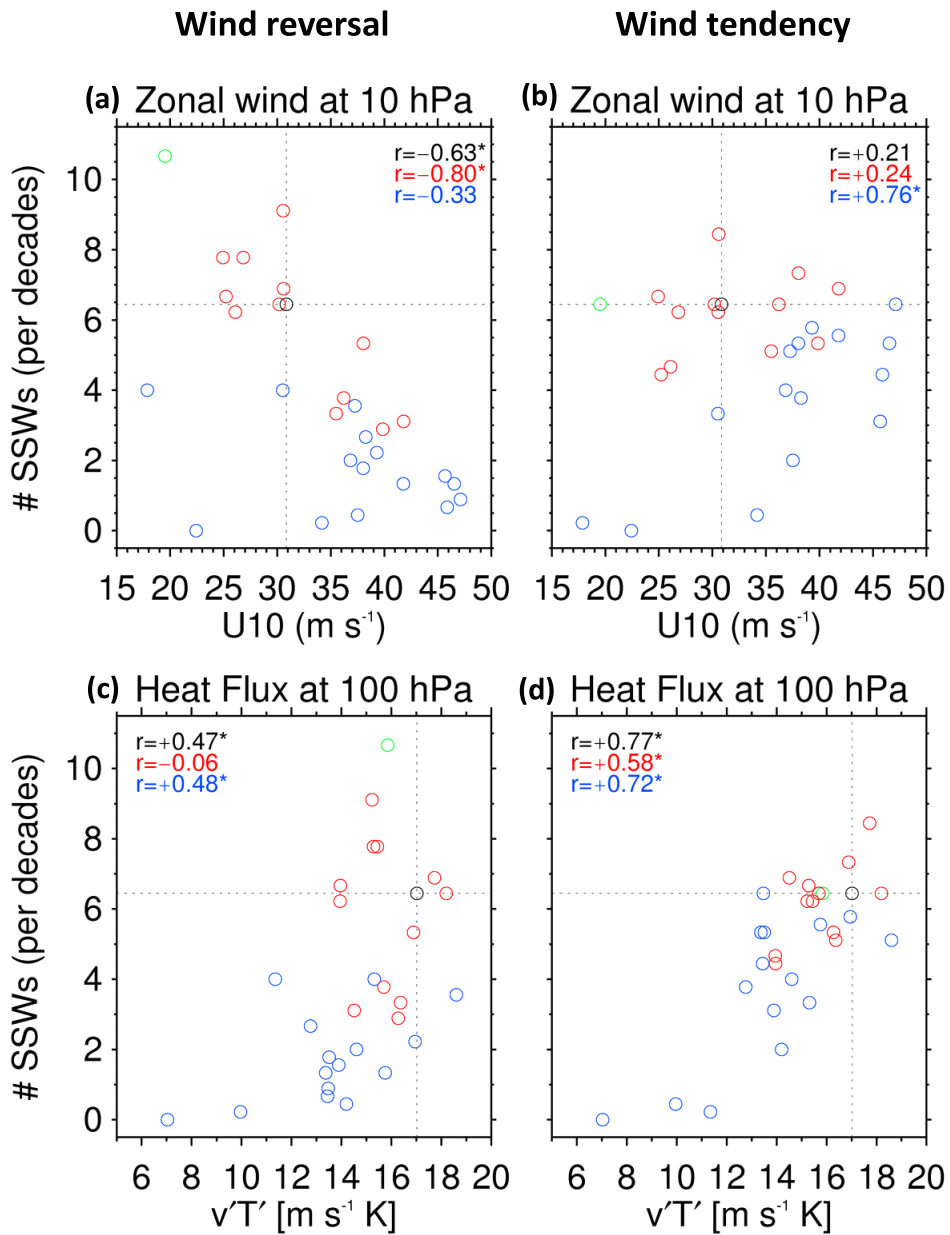


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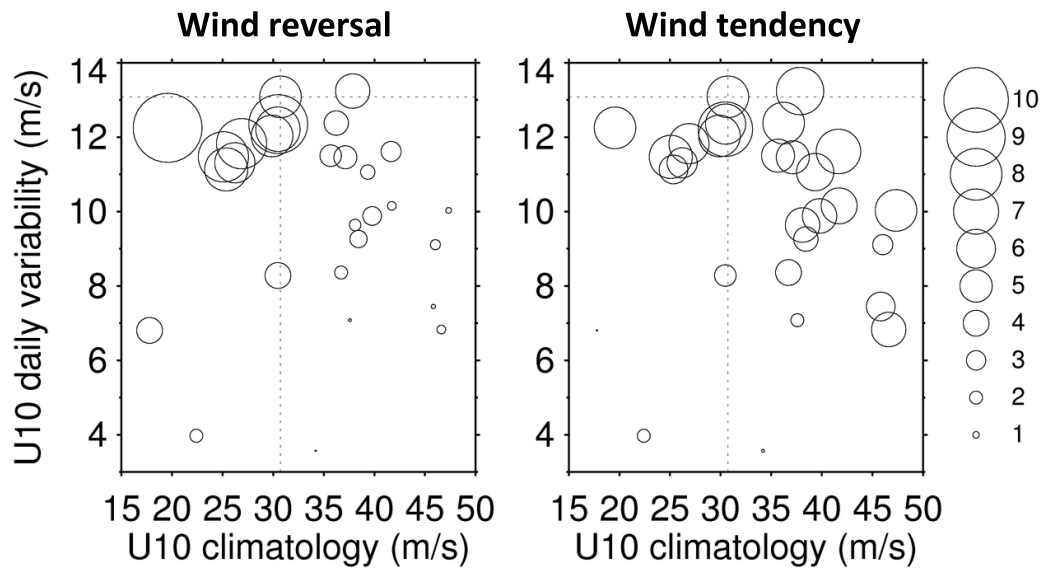


Fig. 8 Same as Fig. 4 but for sudden stratospheric warming (SSW) frequency introduced using the wind reversal definition (left) and the wind tendency definition (right). The circle size indicates the SSW frequency.

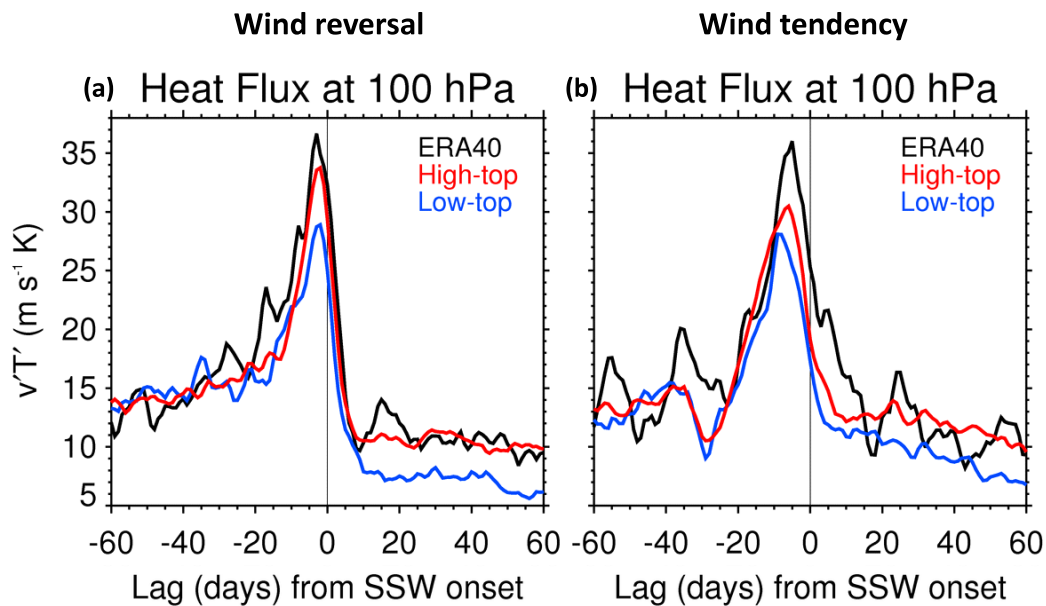


Fig. 9 Multi-model mean time series of zonal-mean eddy heat flux at 100 hPa integrated over 45–75°N during sudden stratospheric warming (SSW) detected by the wind reversal definition (left) and the wind tendency definition (right). Lag zero indicates the onset of SSW. Low-top and high-top models are denoted by blue and red colors, respectively. The reference time series, derived from ERA40, is shown in black.



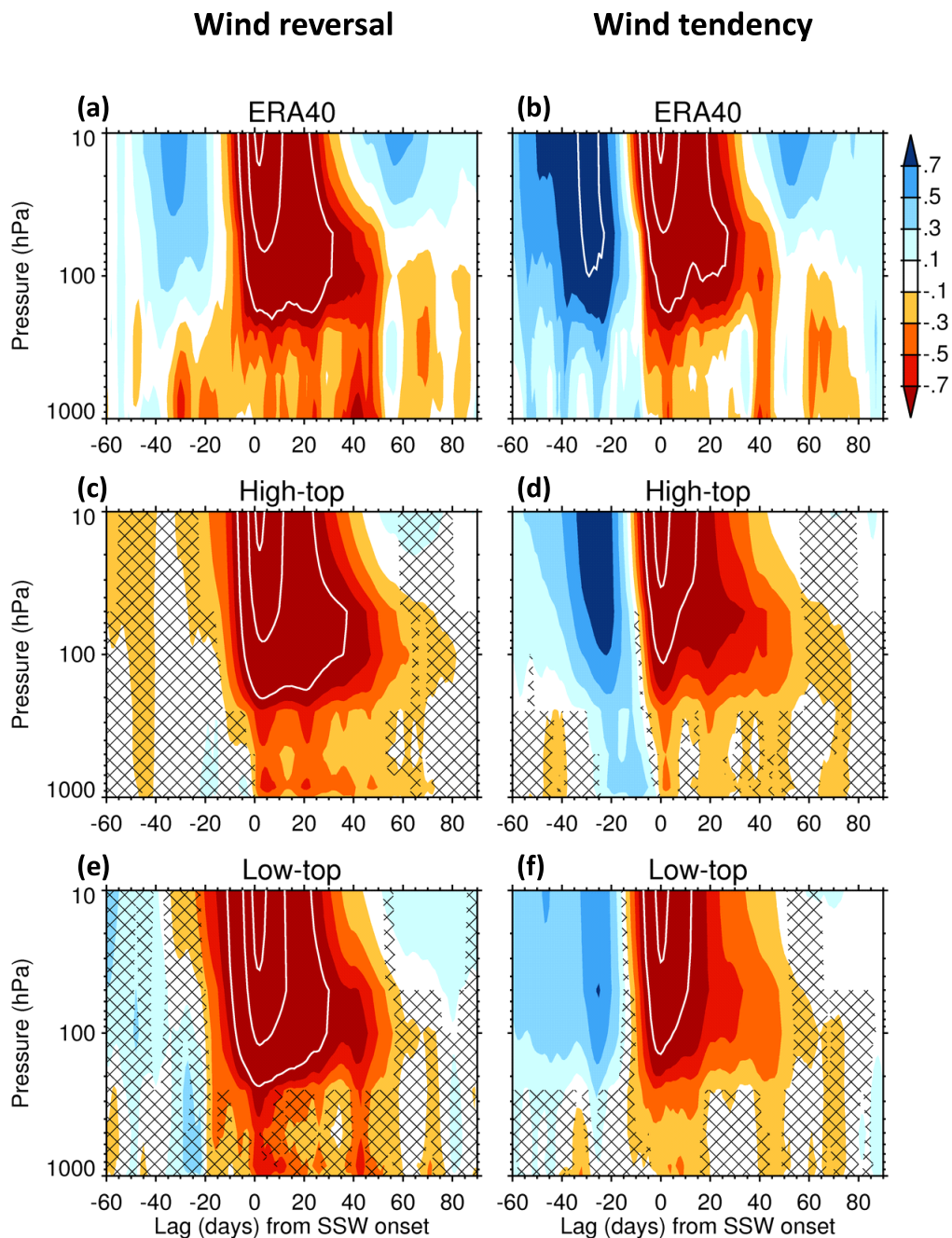


Fig. 10 Time-height development of the northern annular mode (NAM) index during sudden stratospheric warming (SSW) events, as detected by the wind reversal definition (left) and the wind tendency definition (right) for ERA40 (top), high-top (middle), and low-top (bottom) models. The NAM index is based on polar-cap averaged geopotential height ( $>60^{\circ}\text{N}$ ). Shading interval of 1.0 is indicated by a white line. Hatching shows insignificant values (95%) when the multi-model spread is considered.



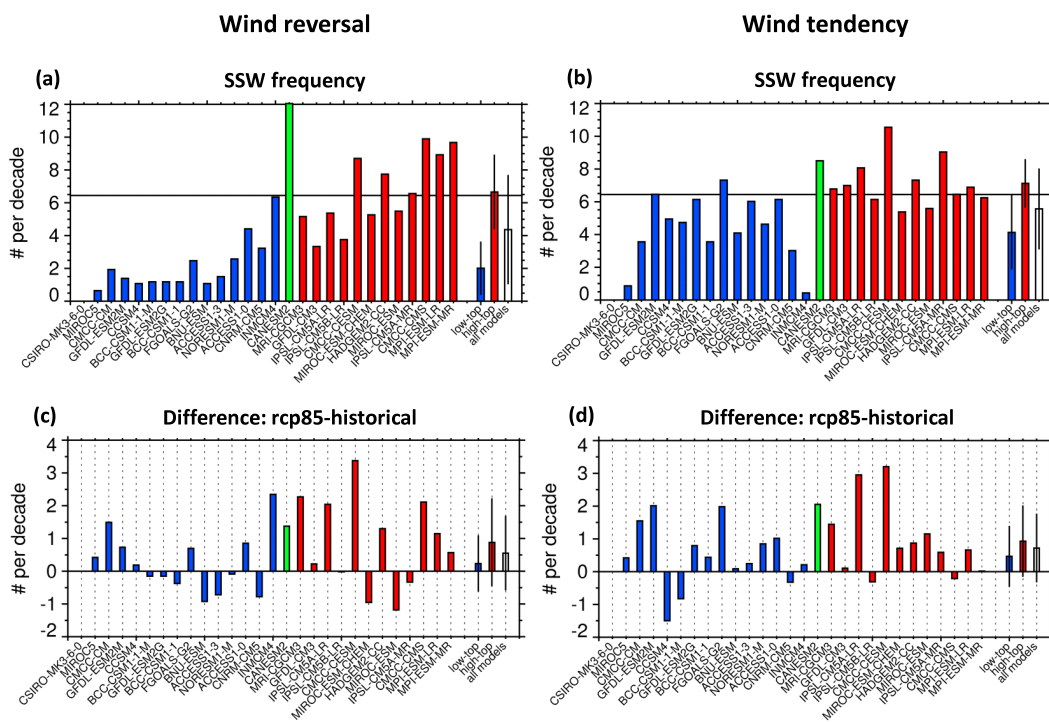


Fig. 11 (Top) Same as Fig. 5 but for RCP8.5 runs. (Bottom) Difference in sudden stratospheric warming (SSW) frequency between RCP8.5 and historical runs.

